Answer the following questions. Answers without proper evidence of knowledge will not be given credit. Make sure to make reasonable simplifications. Do not approximate answers. Give exact answers. No calculators are allowed on this exam.

True or False (2 points each) **1.** $\sqrt{a + b} = \sqrt{a} + \sqrt{b}$ **2.** $(3 \cdot 4)^2 = 3^2 \cdot 4^2$ **3.** $(a + b)^2 = a^2 + b^2$ **4.** $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$ **5.** $\frac{a}{b} + \frac{c}{d} = \frac{a+c}{b+d}$ **6.** $\frac{x+4}{x-4} + \frac{x+5}{x+4} = \frac{(x+4)+(x+5)}{(x-4)+(x+4)}$ **7.** If a function is one-to-one then it is invertible. **8.** $(5^4)^2 = (5^2)^4$

Show your work!

1. (9 points) Which of the following represents a function? (Mark <u>all</u> that apply.) (a) $x^2 + y^2 = 1$ (b) $h = \{(1,2), (5,6), (3,2)\}$ (c) $f(x) = x^3$ 2. Let f(x) = x² + 1 and g(x) = 3x + 7. Evaluate the following and simplify. (5 points each)
a) f ∘ g(x).
b) g ∘ f(x).

3. Let $f(x) = \sqrt{x-3} + 7$, $g(x) = x^3 + 1$ and $h(x) = (x-7)^2$. Evaluate the following functions and find there domains. (You do not need to simplify!) (5 points each)

- a) f + g(x).
- b) $h \cdot g(3)$.
- c) f/h(x).

- 4. Let $j(x) = (x 1)^2 + 3$. Evaluate the following and simplify.
 - a) j(t) (3 points)
 - b) j(3x+1) (7 points)

5. By completing the square, write $f(x) = x^2 + 6x - 4$ in vertex form and state the vertex. (10 points)

6. Determine all possible rational zeroes for the polynomial function $h(x) = 3x^5 + 4x^4 - 3x^2 + 15$. (10 points)

- 7. Use the graphs given below to solve the following inequalities. (5 points each)
 - a) $-x^3 \ge -4x$.
 - b) $x^3 + 4x^2 x 4 < 0$.

8. Find the asymptotes of the graph of $\frac{x^2-2x+1}{x-2}$.

Extra Credit

EC 1. Determine if $f(x) = \frac{\sqrt{3x-1}+7}{2}$ is invertible. If so, find $f^{-1}(x)$. (5 points)

EC 2. Suppose y varies directly as x and inversely as the square of z. If y = 9 when x = 18 and z = 3 then what is the variation constant, k?